

Answer Key

Springs

$$\delta = \frac{8FC^3\eta}{Gd} ; C = \frac{D_m}{d} = \frac{160\text{mm}}{20\text{mm}} = 8$$

from;

$$S_s = \frac{8K_w F D_m}{\pi d^3}$$

$$\text{and; } k_w = \frac{4c-1}{4c-4} + \frac{0.615}{c}$$

$$= \frac{4(8)-1}{4(8)-4} + \frac{0.615}{8}$$

$$k_w = 1.1840$$

subst;

$$150000 \frac{\text{N}}{\text{m}^2} = \frac{8(1.1840)F(0.160\text{m})}{\pi (0.020\text{m})^3}$$

$$F = 2.4875 \text{ kN}$$

Hence;

$$\delta = \frac{8(2.4875\text{ kN})(8)^3(20)}{(80 \times 10^6 \text{ kPa})(0.020\text{m})}$$

$$\delta = 0.1274 \text{ m}$$

$$\delta = 127.4 \text{ mm}$$

$$\delta = \frac{8 F c^3 n}{G d}$$

$$F = m \left(\frac{g_0}{g_c} \right) = 120 \text{ kg} \left(\frac{9.81 \frac{\text{m}}{\text{s}^2}}{1000 \frac{\text{kg} \cdot \text{m}}{\text{N} \cdot \text{s}^2}} \right) = 1.1772 \text{ kN}$$

$$D_m = D_o - d = (0.095 - 0.0095) \text{ m} = 0.0855 \text{ m}$$

$$c = \frac{D_m}{d} = \frac{0.0855 \text{ m}}{0.0095 \text{ m}} = 9$$

$$n = 20 + 2 = 22$$

Subst:

$$\delta = \frac{8 (1.1772 \text{ kN}) (9)^3 (22)}{(95 \times 10^6 \text{ kPa}) (0.0095 \text{ m})}$$

$$\delta = 0.1674 \text{ m}$$

$$\delta = 167.4 \text{ mm}$$

$$k_w = \frac{4C-1}{4C-4} + \frac{0.615}{C}$$

$$C = \frac{D_m}{d} = \frac{D_o + D_i}{2d}$$

$$\text{for } d; \quad d = \frac{D_o - D_i}{2} = \frac{(0.120 - 0.110)\text{m}}{2} = 5 \times 10^{-3} \text{ m}$$

then;

$$C = \frac{(0.120 + 0.110)\text{m}}{2(5 \times 10^{-3} \text{ m})} = 23$$

Hence;

$$k_w = \frac{4(23)-1}{4(23)-4} + \frac{0.615}{23}$$

$$k_w = 1.0608$$

$$S_s = \frac{8k_w F D_m}{\pi d^3}; D_m = c d$$

$$S_s = \frac{8k_w F_c}{\pi d^2}$$

$$\text{from; } k_w = \frac{4c-1}{4c-4} + \frac{0.615}{c}$$

$$= \frac{4(8)-1}{4(8)-4} + \frac{0.615}{8}$$

$$k_w = 1.1840$$

Subst;

$$95000 \frac{\text{lb}}{\text{in}^2} = \frac{8(1.1840)(60165)(8)}{\pi d^2}$$

$$d = 0.1234 \text{ in}$$

$$\frac{1}{k_s} = \frac{1}{k_{s1}} + \frac{1}{k_{s2}} + \frac{1}{k_{s3}}$$

$$\frac{1}{k_s} = \frac{1}{0.3 \text{ kg/mm}} + \frac{1}{0.65 \text{ kg/mm}} + \frac{1}{0.65 \text{ kg/mm}}$$

$$k_s = 0.156 \text{ kg/mm}$$

Hence;

$$k_s = \frac{F}{\delta_T}$$

$$0.156 \text{ kg/mm} = \frac{80 \text{ kg}}{\delta_T}$$

$$\delta_T = 512.8205 \text{ mm}$$

$$S_s = \frac{8 k_w F D_m}{\pi d^3}$$

$$k_w = \frac{4c-1}{4c-4} + \frac{0.615}{c} ; c = \frac{D_m}{d} = \frac{120 \text{ mm}}{13 \text{ mm}} = 9.2308$$

$$= \frac{4(9.2308)-1}{4(9.2308)-4} + \frac{0.615}{9.2308}$$

$$k_w = 1.1577$$

Solving force F that caused solid deflection on spring

$$k_s = \frac{F}{\delta_s} ; \delta_s = F L - S_L$$

$$S_L = (n+2)d$$

$$= (12+2)(13 \text{ mm})$$

$$S_L = 182 \text{ mm}$$

$$\delta_s = (306 - 182) \text{ mm} = 118 \text{ mm}$$

Subst;

$$\frac{130 \text{ kN}}{\text{m}} = \frac{F}{0.118 \text{ m}}$$

$$F = 15.34 \text{ kN}$$

Hence;

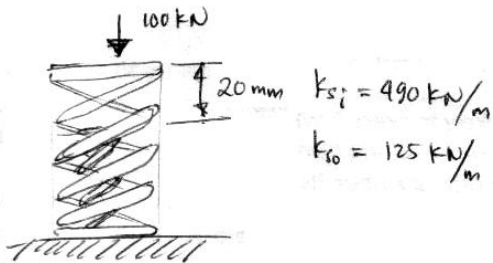
$$S_s = \frac{8(1.1577)(15340 \text{ N})(120 \text{ mm})}{\pi(13 \text{ mm})^3}$$

$$S_s = 2470.0895 \text{ MPa}$$

$$L = \pi D n = \pi (1.2 \text{ in}) (10)$$

$$L = 37.6991 \text{ in}$$

concentric Springs



$$F = F_i + F_o ; \quad k = \frac{F}{\delta} ; \quad \delta_o = \delta_i + 20 \text{ mm}$$

$$100 \text{ kN} = k_i \delta_i + k_o \delta_o$$

$$100 \text{ kN} = k_i \delta_i + k_o (\delta_i + 0.020 \text{ m})$$

$$100 \text{ kN} = \left(490 \frac{\text{kN}}{\text{m}}\right) \delta_i + \left(125 \frac{\text{kN}}{\text{m}}\right) (\delta_i + 0.020 \text{ m})$$

$$\delta_i = 0.1585 \text{ m}$$

then;

$$k_{si} = \frac{F_i}{\delta_{si}}$$

$$490 \frac{\text{kN}}{\text{m}} = \frac{F_i}{0.1585 \text{ m}}$$

$$F_i = 77.6829 \text{ kN}$$

for F_o ;

$$100 \text{ kN} = 77.6829 \text{ kN} + F_o$$

$$F_o = 22.3170 \text{ kN}$$

Hence;

The percent load carried by inner spring

$$\% = \frac{77.6829 \text{ kN}}{100 \text{ kN}} \times 100\%$$

$$\% = 77.68\%$$

$$\delta = \frac{8Fc^3n}{Gd} \quad ; \quad c = \frac{D_m}{d}$$

$$\delta = \frac{8FD_m^3n}{Gd^4}$$

$$80 \text{ mm} = \frac{8(12000 \text{ N}) D_m^3 (15)}{\left(85000 \frac{\text{N}}{\text{mm}^2}\right) (30 \text{ mm})^4}$$

$$d = 156.3905 \text{ mm}$$

$$k_T = \frac{F}{\delta_T} ; \text{ for springs in parallel}$$
$$\delta_T = \delta_1 = \delta_2 = \delta_3 = \delta_4$$
$$k_T = k_{s1} + k_{s2} + k_{s3}$$

$$4 \left(0.725 \frac{\text{kg}}{\text{mm}} \right) = \frac{380 \text{ kg}}{\delta_T}$$

$$\delta_T = 131.0345 \text{ mm}$$

$$\delta_T = \delta_1 + \delta_2 + \delta_3 ; k_s = \frac{F}{\delta} ; F_T = F_1 = F_2 = F_3$$
$$= \frac{80 \text{ Kg}}{0.20 \text{ kg/mm}} + \frac{80 \text{ Kg}}{0.650 \text{ kg/mm}} + \frac{80 \text{ Kg}}{0.650 \text{ Kg/mm}}$$

$$\delta_T = 646.1538 \text{ mm}$$

$$K_s = \frac{F}{\delta} = \frac{30 \text{ kg}}{180 \text{ mm}} = 0.16667 \text{ kg/mm}$$

Hence, the load required for the spring to deflect by 50mm

$$K_s = \frac{F}{\delta}$$

$$0.16667 \text{ kg/mm} = \frac{F}{50 \text{ mm}}$$

$$F = 8.3335 \text{ kg}$$

$$W(h + \delta) = \frac{F}{2} \delta$$

$$120 \text{ lbs} (20 \text{ in} + 5 \text{ in}) = \frac{F}{2} (5 \text{ in})$$

$$F = 1200 \text{ lbs}$$

$$\delta_s = \frac{8 k_w F D_m}{\pi d^3} \quad ; \quad c = \frac{D_m}{d} = \frac{8d}{d} = 8$$

$$k_w = \frac{4c-1}{4c-4} + \frac{0.615}{c}$$

$$= \frac{4(8)-1}{4(8)-4} + \frac{0.615}{8}$$

$$k_w = 1.1840$$

$$\text{from: } E = F \delta$$

$$F = \frac{E}{\delta}$$

$$\text{substit: } \delta_s = \frac{8 k_w E c}{\pi d^2 \delta}$$

$$100000 \frac{\text{lb}}{\text{in}^2} = \frac{8 (1.1840) (300 \text{ ft} \cdot \text{lb}) \left(\frac{12 \text{ in}}{1 \text{ ft}} \right) (8)}{\pi d^2 (5 \text{ in})}$$

$$d = 0.4167 \text{ in}$$

$$k_s = \frac{F}{\delta}$$

$$k_s = \frac{60 \text{ lbs}}{10 \text{ in}} = 6 \text{ lbs/in}$$

Hence; the load that will make the spring deflect by 3 in

$$k_s = \frac{F}{\delta}$$

$$6 \text{ lbs/in} = \frac{F}{3 \text{ in}}$$

$$F = 18 \text{ lbs}$$

$$S_s = \frac{8 k_w F D_m}{\pi d^3} ; c = \frac{D_m}{d}$$

$$S_s = \frac{8 k_w F c}{\pi d^2} ; k_w = \frac{4c-1}{4c-8} + \frac{0.615}{c}$$

$$= \frac{4(9)-1}{4(9)-8} + \frac{0.615}{9}$$

$$k_w = 1.1621$$

Subst;

$$95000 \frac{\text{lb}}{\text{in}^2} = \frac{8(1.1621)(60165)(9)}{\pi d^2}$$

$$d = 0.1297 \text{ in}$$

$$k_s = \frac{F}{\delta} = \frac{60 \text{ lbs}}{6 \text{ in}}$$

$$k_s = 10 \text{ lbs/in}$$

$$\delta = \frac{8FC^3n}{Gd}$$

$$\frac{\delta}{F} = \frac{8C^3n}{Gd} ; C = \frac{D_m}{d} = \frac{80\text{mm}}{12\text{mm}} = 6.6667$$

$$\frac{1}{\frac{40 \frac{\text{kN}}{\text{m}}}{\text{m}}} = \frac{8(6.6667)^3 n}{(85000000 \frac{\text{kN}}{\text{m}})(0.012 \text{ m})}$$

$$n = 10.7577$$

$$k_s = \frac{F}{\delta} ; \delta_s = FL - SL$$

$$FL = nP + d = (16)(12\text{ mm}) + 7\text{ mm} = 199\text{ mm}$$

$$SL = (n+1)d = (16+1)(7\text{ mm}) = 119\text{ mm}$$

$$\delta_s = (199 - 119)\text{ mm} = 80\text{ mm}$$

Hence;

$$\frac{90\text{ kN}}{\text{m}} = \frac{F}{0.080\text{ m}}$$

$$F = 7.2\text{ kN}$$

$$f_s = FL - SL$$

$$FL = nP + 2d = (14)(18\text{ mm}) + 2(12.4\text{ mm}) = 276.8\text{ mm}$$

$$SL = (n+2)d = (14+2)(12.4\text{ mm}) = 198.4\text{ mm}$$

Hence;

$$f_s = (276.8 - 198.4)\text{ mm}$$

$$f_s = 78.4\text{ mm}$$

$$\delta = \frac{12FL^3}{bt^3E(2n_g + 3n_f)} = \frac{12\left(\frac{1200\text{ lbs}}{2}\right)(15\text{ in})^3}{(4\text{ in})(0.20\text{ in})^3(30 \times 10^6\text{ psi})[2(6) + 3(3)]}$$

$$\delta = 1.2054\text{ in}$$

$$S_f = \frac{18FL}{bt^2(2n_g + 3n_f)}$$
$$= \frac{18 \left(\frac{600 \text{ lbs}}{2} \right) (18 \text{ in})}{(3.5 \text{ in}) (0.3 \text{ in})^2 [2(5) + 3(2)]}$$

$$S_f = 19285.7143 \text{ psi}$$