

Answer Key

Physics and Engineering Mechanics 2

$$\dot{V}_F = \frac{2.4 \text{ L}}{12 \text{ min}}$$

$$SG_F = 0.80$$

$$Q_F = 42000 \frac{\text{kJ}}{\text{kg}}$$

$$e = 33\%$$

Find: Brake horse power of the engine

$$e = \frac{BP}{\dot{m}_F Q_F}$$

$$\begin{aligned} \dot{m}_F &= \rho \dot{V} ; SG = \frac{\rho_F}{\rho_W} \\ &= (0.80) \left(1 \frac{\text{kg}}{\text{L}} \right) \left(\frac{2.4 \text{ L}}{12 \text{ min}} \right) \\ \dot{m}_F &= 0.16 \frac{\text{kg}}{\text{min}} \end{aligned}$$

Hence;

$$BP = (0.33) \left(0.16 \frac{\text{kg}}{\text{min}} \right) \left(\frac{1 \text{ min}}{60 \text{ sec}} \right) \left(42000 \frac{\text{kJ}}{\text{kg}} \right)$$

$$BP = (36.96 \text{ kW}) \left(\frac{1 \text{ hp}}{0.746 \text{ kW}} \right)$$

$$BP = 49.5442 \text{ hp}$$

Given: $KE_1 = 28 \text{ J}$

$$KE_2 = 128 \text{ J}$$

$$M = 3.2 \text{ kg}$$

from;

$$\Delta PE = \Delta KE$$

$$m \left(\frac{g_0}{g_c} \right) \Delta z = (KE_2 - KE_1)$$

$$(3.2 \text{ kg}) \left(\frac{9.81 \frac{\text{m}}{\text{s}^2}}{1 \frac{\text{kg} \cdot \text{m}}{\text{N} \cdot \text{s}^2}} \right) \Delta z = (128 - 28) \text{ J}$$

$$\Delta z = 3.1855 \text{ m}$$

$$\dot{V}_F = \left(\frac{6 \text{ gal}}{\text{hr}} \right) \left(\frac{3.78 \text{ L}}{1 \text{ gal}} \right) \left(\frac{1 \text{ hr}}{3600 \text{ s}} \right) = 6.3 \times 10^{-3} \frac{\text{L}}{\text{sec}}$$

$$SG_F = 0.85$$

$$\dot{Q}_F = \left(20300 \frac{\text{Btu}}{\text{lb}} \right) \left(\frac{1.055 \text{ kJ}}{1 \text{ Btu}} \right) \left(\frac{2.2 \text{ lb}}{1 \text{ kg}} \right) = 47116.3 \frac{\text{kJ}}{\text{kg}}$$

$$e = 35\%$$

Find Power output of the engine

$$e = \frac{BP}{\dot{m}_F \dot{Q}_F}$$

$$\dot{m}_F = \rho \dot{V} ; SG = \frac{\rho_F}{\rho_w}$$

$$= (0.85) \left(1 \frac{\text{kg}}{\text{L}} \right) \left(6.3 \times 10^{-3} \frac{\text{L}}{\text{sec}} \right)$$

$$\dot{m}_F = 5.355 \times 10^{-3} \text{ kg/sec}$$

Hence;

$$BP = (0.35) \left(5.355 \times 10^{-3} \frac{\text{kg}}{\text{sec}} \right) \left(47116.3 \frac{\text{kJ}}{\text{kg}} \right)$$

$$BP = 88.3077 \text{ kW}$$

Given: $P = 15 \text{ kW}$

$$e = 82\%$$

$$W = 1550 \text{ lbf}$$

$$e = \frac{P_{out}}{P_{in}} \times 100\%$$

$$0.82 = \frac{P_{out}}{15 \text{ kW}}$$

$$P_{out} = 12.3 \text{ kW}$$

and;

$$W = 1550 \text{ lbf} \left(\frac{4.448 \text{ N}}{1 \text{ lbf}} \right) = 6894.4 \text{ N}$$

Hence;

$$P = F \cdot v$$

$$12300 \frac{\text{J}}{\text{s}} = 6894.4 \text{ N } v$$

$$v = 1.7841 \text{ m/s}$$

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Given: $m = 51 \text{ lbm}$

$r = 3.8 \text{ in}$

$N = 1400 \text{ rpm}$

Find: KE

$$KE = \frac{1}{2} \frac{m}{g_c} v^2$$

$$v = 2\pi r N$$
$$= 2\pi (3.8 \text{ in}) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) \left(\frac{1400 \text{ rpm}}{60} \right)$$

$$v = 46.4258 \text{ ft/sec}$$

subst:

$$KE = \frac{1}{2} \left(\frac{51 \text{ lbm}}{32.2 \frac{\text{ft-lb}}{\text{lbm-sec}^2}} \right) (46.4258 \text{ ft/sec})^2$$

$$KE = 167.3409 \text{ ft-lb}$$

Given: $v = \left(70 \frac{\text{miles}}{\text{hr}}\right) \left(\frac{5280 \text{ ft}}{1 \text{ mile}}\right) \left(\frac{1 \text{ hr}}{3600 \text{ sec}}\right) = 102.6667 \text{ ft/sec}$

$$m = 1200 \text{ lb}$$

$$KE = \frac{1}{2} \frac{m}{g_c} v^2 = \frac{1}{2} \left(\frac{1200 \text{ lb}}{32.2 \frac{\text{ft-lb}}{\text{lb}_m \cdot \text{sec}^2}} \right) (102.6667 \text{ ft/sec})^2$$

$$KE = 196405.9246 \text{ lb-ft}$$

$$m_A = 12\text{ g} \quad m_B = 12\text{ g}$$

$$v_A = 18\text{ m/s} \quad v_B = 95\text{ m/s}$$

$$m_A v_A + m_B v_B = m_A' v_A' + m_B' v_B'$$

$$\text{note: } v_A' = v_B' = v'$$

$$(12\text{ g})(18\text{ m/s}) + (12\text{ g})(95\text{ m/s}) = v'(12 + 12)\text{ g}$$

$$v' = 56.5\text{ m/s}$$

Given: $m = 1100 \text{ slugs}$

$t = 15 \text{ sec}$

$v_f = 28 \text{ ft/sec}$

Required: Resultant force;

$$m = (1100 \text{ slugs}) \left(\frac{32.2 \text{ lb}_m}{1 \text{ slug}} \right) \left(\frac{32.2 \text{ ft/sec}^2}{32.2 \frac{\text{lb-ft}}{\text{lb-sec}^2}} \right) = 35420 \text{ lb}_f$$

$$v_f = v_i + at$$

$$28 \text{ ft/sec} = a(15 \text{ sec})$$

$$a = 1.8667 \text{ ft/sec}^2$$

Hence; From 2nd Law of motion

$$F_R = m \left(\frac{a_0}{a_c} \right) = 35420 \text{ lb}_m \left(\frac{1.8667 \text{ ft/sec}^2}{32.2 \frac{\text{lb-ft}}{\text{lb-sec}^2}} \right)$$

$$F_R = 2053.37 \text{ lb}_f$$

let v = speed of coupled cars
By conservation of momentum

$$M_1 V_1 + M_2 V_2 = m_1 v_1' + m_2 v_2'$$

$$(50 \text{ ton}) \left(1.5 \frac{\text{mile}}{\text{hr}} \right) + (80 \text{ ton})(0) = 50 v + 80 v$$

$$v = 0.5770 \text{ mi/hr}$$

$$h_L = f \frac{L v^2}{2gD}$$

$$Q = A v$$

$$\left(4100 \frac{\text{gal}}{\text{min}} \right) \left(\frac{1 \text{ min}}{60 \text{ sec}} \right) \left(\frac{1 \text{ ft}^3}{7.48 \text{ gal}} \right) = \frac{\pi}{4} (1.4 \text{ ft})^2 v$$

$$v = 5.9337 \text{ ft/sec}$$

Subst;

$$h_L = 0.0157 \frac{(260 \text{ ft})(5.9337 \text{ ft/sec})^2}{2(32.2 \text{ ft/sec}^2)(1.4 \text{ ft})} = 1.5941 \text{ ft}$$

Hence;

$$P = \gamma h_L = (62.4 \frac{\text{lb}}{\text{ft}^3})(1.5941 \text{ ft})$$

$$P = 99.4706 \frac{\text{lb}}{\text{ft}^2}$$

$$Q = m C_p \Delta T$$
$$= 3 \frac{\text{kg}}{\text{s}} (4.187 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}) (95 - 34)^\circ \text{C}$$

$$Q = 766.221 \text{ kW}$$

and:

$$0.75 P = Q$$

$$0.75 P = 766.221 \text{ kW}$$

$$P = 1021.628 \text{ kW}$$

Hence;

$$P = VI$$

$$1021.628 \times 10^3 \text{ W} = (2000 \text{ V}) I$$

$$I = 510.814 \text{ amp}$$

$$P = VI = I^2 R$$

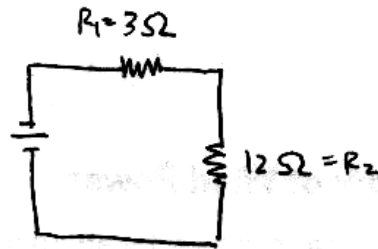
$$1200 \text{ W} = I^2 (12 \text{ ohms})$$

$$I = 10 \text{ amp}$$

$$\text{Power factor} = \frac{\text{kW}}{\text{kVA}} \\ = \frac{(220\text{V})(11\text{A})}{2600\text{VA}}$$

$$\text{Power Factor} = 0.9308$$

$$\text{Power Factor} = 93.08\%$$



$$R_T = R_1 + R_2 = 15\Omega$$

$$I_T = I_1 = I_2 = \frac{V_T}{R_T} = \frac{450V}{15\Omega} = 30 \text{ amps}$$

Hence;

$$\begin{aligned} V_2 &= I_2 R_2 \\ &= (30 \text{ amps})(3\Omega) \end{aligned}$$

$$V_2 = 90V$$

$$\frac{V_1}{V_2} = \frac{N_1}{N_2}$$

$$\frac{200V}{V_2} = \frac{280 \text{ turns}}{50 \text{ turns}}$$

$$V_2 = 35.7143 \text{ V}$$

$$C = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2}}$$

$$7.6 \mu F = \frac{1}{\frac{1}{9.8 \mu F} + \frac{1}{C_2}}$$

$$C_2 = 33.8545 \mu F$$

$$\begin{aligned} P &= VI \\ &= (230\text{V})(18\text{A}) \\ P &= (4140\text{ W})\left(\frac{1\text{hp}}{746\text{ W}}\right) \end{aligned}$$

$$P = 5.5496\text{ hp}$$

$$Q = It$$

$$630 \text{ coulombs} = I (18 \text{ sec})$$

$$I = 35 \text{ amps}$$

$$\tan \theta = \frac{v^2}{gr}$$

$$\tan 9^\circ = \frac{(20 \text{ m/s})^2}{(9.81 \text{ m/s}^2)r}$$

$$r = 257.4414 \text{ m}$$

$$\tan \theta = \frac{v^2}{gr} = \frac{\left[(60 \text{ miles/hr}) \left(\frac{1 \text{ hr}}{3600 \text{ sec}} \right) \left(\frac{5280 \text{ ft}}{1 \text{ mile}} \right) \right]^2}{(32.2 \text{ ft/sec}^2)(1800 \text{ ft})}$$

$$\tan \theta = 0.1336$$

$$\theta = 7.6102^\circ$$

$$\rho_o V_o = \rho_F V_d$$
$$(0.75)(62.4 \frac{\text{lb}}{\text{ft}^3}) \left[(1.5 \text{ in}^2) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2} \right) (28 \text{ in}) \left(\frac{1 \text{ ft}}{12 \text{ in}} \right) \right] = (62.4 \frac{\text{lb}}{\text{ft}^3}) \left[(L)(1.5 \text{ in}^2) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2} \right) \right]$$

$$L = (1.75 \text{ ft}) \left(\frac{12 \text{ in}}{1 \text{ ft}} \right)$$

$$L = 21 \text{ ft}$$

$$\frac{P_1 - P_2}{\gamma} = \frac{v_2^2 - v_1^2}{2g_0}$$

$$m = \rho_1 A_1 v_1$$

$$100 \frac{\text{lb}}{\text{sec}} = 62.4 \frac{\text{lb}}{\text{ft}^3} \left(\frac{\pi}{4} \right) (\sin)^2 \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2} \right) v_1$$

$$v_1 = 11.7529 \text{ ft/sec}$$

$$m = \rho_2 A_2 v_2$$

$$100 \frac{\text{lb}}{\text{sec}} = 62.4 \frac{\text{lb}}{\text{ft}^3} \left(\frac{\pi}{4} \right) (1.0)^2 \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2} \right) v_2$$

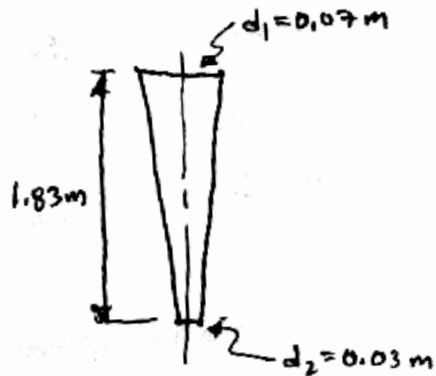
$$v_2 = 293.8245 \text{ ft/sec}$$

Hence;

$$\Delta P = \frac{(293.8245^2 - 11.7529^2) \text{ ft}^2/\text{sec}^2}{2(32.2 \text{ ft/sec}^2)} (62.4 \text{ lb/ft}^3)$$

$$\Delta P = (8357.8519 \text{ lb/ft}^2) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2} \right)$$

$$\Delta P = 579.9851 \text{ psi}$$



$$Q = A_1 v_1$$

$$0.03 \text{ m}^3/\text{s} = \frac{\pi}{4} (0.07 \text{ m})^2 v_1$$

$$v_1 = 7.7953 \text{ m/s}$$

$$Q = A_2 v_2$$

$$0.03 \text{ m}^3/\text{s} = \frac{\pi}{4} (0.03 \text{ m})^2 v_2$$

$$v_2 = 42.4413 \text{ m/s}$$

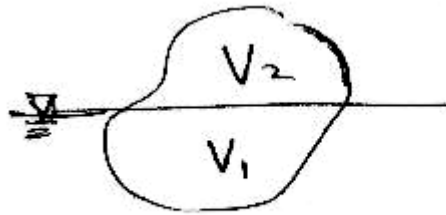
Subst;

$$\Delta P = \left[\frac{(42.4413^2 - 7.7953^2) \text{ m}^2/\text{s}^2}{2(9.81 \text{ m/s}^2)} - 1.83 \text{ m} \right] (9.81 \text{ kN/m}^3)$$

$$\Delta P = 852.2963 \text{ kPa}$$

$$\frac{P_1}{\gamma} + \frac{v_1^2}{2g_0} + z_1 = \frac{P_2}{\gamma} + \frac{v_2^2}{2g_0} + z_2^0$$

$$P_2 - P_1 = \left[\frac{v_2^2 - v_1^2}{2g_0} - z_1 \right] \gamma$$



$$BF = W$$

$$(13.6) \left(9.81 \frac{\text{KN}}{\text{m}^3} \right) V_1 = (7.8) \left(9.81 \frac{\text{KN}}{\text{m}^3} \right) V_T$$

$$V_1 = 0.5735 V_T$$

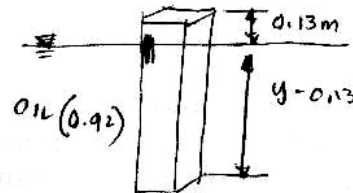
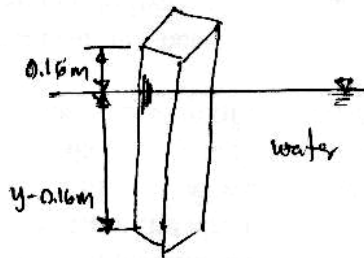
$$\text{but: } V_T = V_1 + V_2$$

$$V_T = 0.5735 V_T + V_2$$

$$V_2 = 0.4265 V_T$$

Hence;

$$\boxed{\frac{V_2}{V_T} = 0.4265}$$



Value of "y"

$$W = (9.81 \text{ kN/m}^3)(0.15 \text{ m})(0.15 \text{ m})(y - 0.16 \text{ m})$$

$$W_w = 2.4525 (y - 0.16 \text{ m})$$

$$W = (9.81 \text{ kN/m}^3)(0.92)(0.15 \text{ m})(0.15 \text{ m})(y - 0.13 \text{ m})$$

$$W_o = 2.2563 (y - 0.13 \text{ m})$$

$$W_w = W_o$$

$$2.4525 (y - 0.16 \text{ m}) = 2.2563 (y - 0.13 \text{ m})$$

$$1.08696 y - 0.17391 \text{ m} = y - 0.13 \text{ m}$$

$$y = 0.5049 \text{ m}$$