

Answer Key

Refrigeration System

$$\text{COP} = \frac{Q_A}{W_i} = \frac{Q_A}{Q_R - Q_A}$$

$$5 = \frac{(80 \times 3.516) \text{ kW}}{Q_R - (80 \times 3.516) \text{ kW}}$$

$$Q_R = 337.536 \text{ kW}$$

then;

$$Q_R = m C_p \Delta T$$

$$337.536 \text{ kW} = m (4.187 \text{ kJ/kg} \cdot \text{K}) (10^\circ\text{C})$$

$$m = 8.0615 \text{ kg/s}$$

Hence;

$$\rho = \frac{m}{V}$$

$$1000 \text{ kg/m}^3 = \frac{8.0615 \text{ kg/s}}{V}$$

$$\dot{V} = (8.0615 \times 10^{-3} \frac{\text{m}^3}{\text{s}}) \left(\frac{1000 \text{ L}}{1 \text{ m}^3} \right) \left(\frac{1 \text{ gal}}{3.78 \text{ L}} \right) \left(\frac{60 \text{ s}}{1 \text{ min}} \right)$$

$$\dot{V} = 127.9607 \text{ gal/min}$$

$$Q_A = (8.5 \text{ tons}) \left(\frac{3.516 \text{ kW}}{1 \text{ ton}} \right) = 298.86 \text{ kW}$$

$$\text{COP} = \frac{Q_A}{W_c}$$

$$4.5 = \frac{298.86 \text{ kW}}{W_c}$$

$$W_c = 66.4133 \text{ kW}$$

$$\text{then, } \eta_c = \frac{W_c}{EP}$$

$$0.75 = \frac{66.4133 \text{ kW}}{EP}$$

$$EP = 88.55 \text{ kW}$$

$$\text{COP} = \frac{T_L}{T_H - T_L} = \frac{270 \text{ K}}{318 \text{ K} - 270 \text{ K}}$$

$$\text{COP} = 5.625$$

Then;

$$\text{COP} = \frac{Q_A}{W_c}$$

$$5.625 = \frac{Q_A}{(50 \text{ kW}) \left(\frac{1 \text{ ton}}{3.516 \text{ kW}} \right)}$$

$$Q_A = 80 \text{ tons}$$

$$\dot{Q}_A = \dot{m}_R (h_1' - h_4)$$

$$80 \text{ kW} = \dot{m}_R (1475 - 360.1) \text{ kJ/kg}$$

$$\dot{m}_R = 0.07176 \text{ kg/s}$$

And;

$$\dot{Q}_R = \dot{m}_R (h_2 - h_3')$$

$$= (0.07176 \text{ kg/s}) (1720 - 360.1) \text{ kJ/kg}$$

$$\dot{Q}_R = 97.58 \text{ kW}$$

then;

$$\dot{Q}_R = \dot{m} (c_p \Delta T)$$

$$97.58 \text{ kW} = \dot{m} (4.187 \text{ kJ/kg}) (7^\circ\text{C})$$

$$\dot{m} = (3.3294 \text{ kg/s}) \left(\frac{3600 \text{ s}}{1 \text{ hr}} \right)$$

$$\dot{m} = 11985.6763 \text{ kg/hr}$$

$$A_v = 1 + c - c \left(\frac{P_2}{P_1} \right)^{1/\eta} = \frac{V'}{V_0} ; r_k = \left(\frac{P_2}{P_1} \right)^{1/\eta} = \frac{V_1}{V_2}$$

$$1 + 0.09 - 0.09(6.5) = \frac{(0.20 \text{ m}^3/\text{s})}{V_0}$$

$$V_0 = 0.3960 \text{ m}^3/\text{s}$$

Then;

$$V_0 = \frac{\pi D^2}{4} L \frac{N}{60} ; D = L$$

$$0.3960 \text{ m}^3/\text{s} = \frac{\pi D^3}{4} \left(\frac{350 \text{ rpm}}{60} \right)$$

$$D = 0.4422 \text{ m}$$

$$D = 442.1578 \text{ mm}$$

Heat pump

$$P.F. = \frac{T_H}{T_H - T_L} = \frac{298\text{ K}}{298\text{ K} - 268\text{ K}}$$

$$P.F. = 10$$

Heat pump

$$\text{P.F.} = \frac{Q_R}{W_L} = \frac{65 \text{ kW}}{15 \text{ kW}} = 4.33$$

Then;

$$\text{P.F.} = \frac{T_H}{T_H - T_L}$$

$$4.33 = \frac{323 \text{ K}}{323 \text{ K} - T_L}$$

$$T_L = 248.4042 \text{ K}$$

$$t_L = -24.5958^\circ\text{C}$$

Heat pump

$$P.F. = \frac{Q_R}{W_c} = \frac{T_H}{T_H - T_L} = \frac{588^\circ R}{588^\circ R - 497^\circ R} = 6.4615$$

then;

$$6.4615 = \frac{489 \text{ Btu/min}}{W_c}$$

$$W_c = (75.6786 \text{ Btu/min}) \left(\frac{1.065 \text{ kJ}}{1 \text{ Btu}} \right) \left(\frac{1 \text{ min}}{60 \text{ s}} \right) \left(\frac{1 \text{ hp}}{0.746 \text{ kW}} \right)$$

$$W_c = 1.80 \text{ hp}$$

Heat pump

$$P.F. = \frac{Q_R}{W_C} = \frac{T_H}{T_H - T_L}$$

$$\frac{Q_R}{\left(\frac{8 \text{ kJ}}{\text{s}}\right) \left(\frac{60 \text{ s}}{1 \text{ min}}\right)} = \frac{306 \text{ K}}{306 \text{ K} - 268 \text{ K}}$$

$$Q_R = 3865.2632 \text{ kJ/min}$$

then;

$$W_C = Q_R - Q_A$$

$$\left(\frac{8 \text{ kJ}}{\text{s}}\right) \left(\frac{60 \text{ s}}{1 \text{ min}}\right) = 3865.2632 \text{ kJ/min} - Q_A$$

$$Q_A = 3385.2632 \text{ kJ/min}$$

Degree of Superheat

$$^{\circ}\text{SH} = t_1 - t_{\text{evap}}$$

└── temp. in evaporator
└── temp. entering compressor

$$^{\circ}\text{SH} = (10 + 6)^{\circ}\text{C}$$

$$^{\circ}\text{SH} = 16^{\circ}\text{C}$$

$$^{\circ}\text{SH} = 60.8^{\circ}\text{F}$$

$$P_i = \sqrt{(90 \text{ kPa})(110 \text{ kPa})}$$

$$P_i = 298.4962 \text{ kPa}$$

$$Q_A = m C_p \Delta T$$

$$(20 \text{ ton}) \left(\frac{3.516 \text{ kW}}{1 \text{ ton}} \right) = m (4.187 \text{ kJ/kg} \cdot \text{K}) (30 + 8) \text{ K}$$

$$m = \left(0.44197 \text{ kg/s} \right) \left(12 \text{ hrs} \right) \left(\frac{3600 \text{ s}}{1 \text{ hr}} \right)$$

$$m = 19\,093.0826 \text{ kg}$$

LOAD w/ Freezing

$$Q_A = \frac{m_p}{t} \left[C_{p1} (t_1 - t_f) + L + C_{p2} (t_f - t_2) \right]$$

$$= \frac{12000 \text{ kg}}{(12 \text{ hrs}) \left(\frac{3600 \text{ s}}{1 \text{ hr}} \right)} \left[(3.82 \text{ kJ/kg} \cdot \text{K}) (30 + 1)^\circ\text{C} + 281 \text{ kJ/kg} + (1.9 \text{ kJ/kg} \cdot \text{K}) (-1 + 5)^\circ\text{C} \right]$$

$$Q_A = (108.8389 \text{ kW}) \left(\frac{1 \text{ ton}}{3.516 \text{ kW}} \right)$$

$$Q_A = 30.9553 \text{ tons}$$

$$Q = m C_p \Delta T = (9 \text{ kg/s}) (4.187 \text{ kJ/kg} \cdot \text{K}) (31 - 3)^\circ\text{C}$$

$$Q = (1055.124 \text{ kW}) \left(\frac{1 \text{ ton}}{3.516 \text{ kW}} \right)$$

$$Q = 300 \text{ tons}$$

Heat pump

$$PF = \frac{T_H}{T_H - T_L} = \frac{(48 + 273) \text{ K}}{[321 - (-6 + 273)] \text{ K}}$$

$$PF = 6.0$$

$$W_L = m_R (h_2 - h_1)$$

$$\dot{Q} = m_R (h_1 - h_4)$$

$$12 \text{ kW} = m_R (350.1 - 241.6) \text{ kJ/kg}$$

$$m_R = 0.1106 \text{ kg/s}$$

then;

$$W_L = (0.1106 \text{ kg/s}) (378 - 350.1) \text{ kJ/kg}$$

$$W_L = 3.0857 \text{ kW}$$

$$Q_R = m (h_2 - h_3)$$

$$Q_A = m (h_1 - h_4)$$

$$(55 \text{ ton}) \left(\frac{3.516 \text{ kW}}{1 \text{ ton}} \right) = m (407 - 255) \text{ kJ/kg}$$

$$m = 1.2722 \text{ kg/s}$$

Subst,

$$Q_R = (1.2722 \text{ kg/s}) (448 - 255) \text{ kJ/kg}$$

$$Q_R = 245.5417 \text{ kW}$$