

Answer Key

Pure Substance, Rankine Cycle and
Geothermal Power Plant

$m = 25 \text{ kg}$ @ 55°C saturated

$$\bar{v} = \frac{V}{m}$$

$$V = \bar{v} m$$

$$\rightarrow \bar{v}_{\text{g}} @ 55^\circ\text{C} = 9568 \times 10^{-3} \text{ m}^3/\text{kg}$$

$$V = (9568 \times 10^{-3} \text{ m}^3/\text{kg}) (25 \text{ kg})$$

$$V = 239.2 \text{ m}^3$$

STEAM TABLES:

$$S = S_f + X S_{fg}$$

Diagram illustrating the steam state and entropy values:

- Vertical line representing the saturation curve.
- Horizontal line from the vertical line to the right, labeled $S_{fg} @ 190^\circ\text{C} = 4.2720 \text{ kJ/kg-K}$.
- Horizontal line from the vertical line to the right, labeled $S_f @ 190^\circ\text{C} = 2.2359 \text{ kJ/kg-K}$.
- Horizontal line from the vertical line to the right, labeled 5.5 kJ/kg-K .

$$X = 76.40\%$$

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STEAM TABLES

$$V_f = 25 \text{ L}$$

$$m_f = 10 \text{ kg}$$

$$m_f = \frac{V_f}{v_{f@250^\circ\text{C}}}$$

$$10 \text{ kg} = \frac{V_f}{(1.2512 \times 10^{-3} \text{ m}^3/\text{kg})}$$

$$V_f = 0.01251 \text{ m}^3 \text{ (volume of liquid)}$$

and;

$$m_g = \frac{V_g}{v_{g@250^\circ\text{C}}} = \frac{(0.025 - 0.01251) \text{ m}^3}{(50.13 \times 10^{-3} \text{ m}^3/\text{kg})}$$

$$m_g = 0.2491 \text{ kg} \text{ (mass of vapor)}$$

therefore;

$$x = \frac{m_g}{m_f + m_g} = \frac{0.2491 \text{ kg}}{(10 + 0.2491) \text{ kg}}$$

$$x = 2.4305 \% \text{ (vapor content)}$$

hence; the moisture content

$$y = (100 - 2.4305) \%$$

$$y = 97.57 \%$$

$$h = m C_p t = (4187 \text{ kJ/kg} \cdot \text{K})(45^\circ \text{C})$$

$$h = 188.415 \text{ kJ/kg}$$

$$h = m C_p t$$

$$C_p = \left(4.187 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} - k \right) \left(\frac{0.24 \frac{\text{Btu}}{\text{lbm} \cdot ^\circ\text{R}}}{1.0062 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}} \right)$$

$$C_p = 0.9987 \frac{\text{Btu}}{\text{lbm} \cdot ^\circ\text{R}}$$

$$h = (0.9987 \frac{\text{Btu}}{\text{lbm} \cdot ^\circ\text{R}})(200^\circ\text{F})$$

$$h = 199.74 \frac{\text{Btu}}{\text{lbm}}$$

$$m_f = \frac{V_f}{\bar{v}_f @ 120 \text{ kPa}} = \frac{6 \text{ m}^3}{1.0473 \times 10^{-3} \text{ m}^3/\text{kg}} = 5729.0175 \text{ kg}$$

$$m_g = \frac{V_g}{\bar{v}_g @ 120 \text{ kPa}} = \frac{6 \text{ m}^3}{1428.4 \times 10^{-3} \text{ m}^3/\text{kg}} = 4.20 \text{ kg}$$

$$x = \frac{m_g}{m_f + m_g} = \frac{4.20 \text{ kg}}{(5729.0175 + 4.20) \text{ kg}} = 7.3257 \times 10^{-4}$$

Hence;

$$u = u_f + x u_{fg}$$

$$u = u_f + x (u_g - u_f)$$

$$u_f @ 120 \text{ kPa} = 439.20 \text{ kJ/kg}$$

$$u_g @ 120 \text{ kPa} = 2512.1 \text{ kJ/kg}$$

$$u = (440.7185 \text{ kJ/kg}) (5729.0175 + 4.20) \text{ kg}$$

$$u = 2.5267 \times 10^6 \text{ kJ}$$

$$h_2 - h_1 = m C_p (T_2 - T_1)$$
$$(2599.1 - 2592.1) \text{ kJ/kg} = C_p (53.97 - 50)^\circ\text{C}$$

$$C_p = 1.7632 \text{ kJ/kg}\cdot^\circ\text{C}$$

$$m_f = 1.2 \text{ kg}$$

$$V_f = m_f \bar{v}_f$$

$$\rightarrow \bar{v}_f @ 620 \text{ kPa} = 1.1021 \times 10^{-3} \text{ m}^3/\text{kg}$$

$$V_f = (1.2 \text{ kg})(1.1021 \times 10^{-3} \text{ m}^3/\text{kg}) = 1.3225 \times 10^{-3} \text{ m}^3$$

and;

$$V_g = V_T - V_f = (1.5 - 1.3225 \times 10^{-3}) \text{ m}^3$$

$$V_g = 1.4987 \text{ m}^3$$

Hence;

$$m_g = \frac{V_g}{\bar{v}_g} = \frac{1.4987 \text{ m}^3}{306 \times 10^{-3} \text{ m}^3/\text{kg}}$$

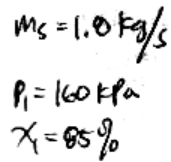
$$m_g = 4.8976 \text{ kg}$$

$$\begin{aligned} S &= S_f + x S_{fg} \\ &= 0.4417 \text{ Btu/lb-}^\circ\text{R} + (0.70)(1.6288 - 0.4417) \text{ Btu/lb-}^\circ\text{R} \\ S &= 1.2727 \text{ Btu/lb-}^\circ\text{R} \end{aligned}$$

$$Q = m C_v \Delta T$$

$$(310 \text{ Btu}) \left(\frac{1.055 \text{ kJ}}{1 \text{ Btu}} \right) = (1 \text{ kg}) (4.2 \text{ kJ/kg} \cdot \text{K}) \Delta T$$

$$\Delta T = 77.8690 \text{ K}$$



$$m_s(h_1 - h_2) = m_w C_p \Delta T$$

$$h_1 = h_f + X_1 h_{fg}$$

$\downarrow$ $\downarrow$
 $h_f @ 160 \text{ kPa} = 975.36 \text{ kJ/kg}$ $h_{fg} @ 160 \text{ kPa} = 2221.1 \text{ kJ/kg}$

$$h_2 = h_f @ 160 \text{ kPa} = 475.36 \text{ kJ/kg}$$

$$(1.8 \text{ kg/s}) (2363.295 - 435.36) \text{ kJ/kg} = m_w (4.187 \text{ kJ/kg} \cdot ^\circ\text{C} - T) (15^\circ\text{C})$$

$$m_w = 54.1085 \text{ kg/s}$$

FACTOR OF EVAPORATION

$$F.E. = \frac{h_g - h_f}{2257}$$

$$1.3 = \frac{h_g - h_f}{2257}$$

$$h_g - h_f = 2934.1 \text{ kJ/kg}$$

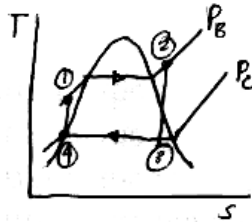
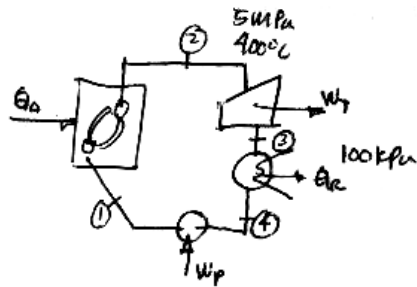
then,

$$\eta_{th} = \frac{W_{net}}{E_{in}} = \frac{W_{net}}{m_s (h_g - h_f)}$$

$$0.70 = \frac{6000 \text{ kW}}{m_s (2934.1 \text{ kJ/kg})}$$

$$m_s = (2.9213 \text{ kg/s}) \left(\frac{3600 \text{ s}}{1 \text{ hr}} \right)$$

$$m_s = 10516.7318 \text{ kg/hr}$$



$$\eta_{th} = \frac{Q_{in} - Q_{R}}{Q_{in}} = 1 - \frac{Q_{R}}{Q_{in}} = 1 - \frac{h_3 - h_4}{h_2 - h_1}$$

@ 5 MPa & 400°C

$$h_2 = 3195.7 \text{ kJ/kg}$$

$$s_2 = 6.6459 \text{ kJ/kg-K}$$

$$s_2 = s_f + x_3 s_{fg}$$

$$\begin{aligned} & \rightarrow s_{fg} @ 0.1 \text{ MPa} = 6.0568 \text{ kJ/kg-K} \\ & \rightarrow s_f @ 0.1 \text{ MPa} = 1.3026 \text{ kJ/kg-K} \end{aligned}$$

$$x_3 = 0.8821$$

$$h_3 = h_f + x_3 h_{fg}$$

$$\rightarrow h_{fg} @ 0.1 \text{ MPa} = 2358.0 \text{ kJ/kg}$$

$$\rightarrow h_f @ 0.1 \text{ MPa} = 417.46 \text{ kJ/kg}$$

$$h_3 = 2497.4518 \text{ kJ/kg}$$

$$h_4 = h_f @ 0.1 \text{ MPa} = 417.46 \text{ kJ/kg}$$

$$h_1 - h_4 = \bar{v}_4 (p_1 - p_4)$$

$$\rightarrow \bar{v}_4 = \bar{v}_f @ 0.1 \text{ MPa} = 1.0432 \times 10^{-3} \text{ m}^3/\text{kg}$$

$$h_1 = 422.5717 \text{ kJ/kg}$$

Therefore;

$$\eta_{th} = 1 - \frac{(2497.4518 - 417.46) \text{ kJ/kg}}{(3195.7 - 422.5717) \text{ kJ/kg}} \times 100\%$$

$$\boxed{\eta_{th} = 25\%}$$

$$W_T' = 650 \text{ kJ/kg}, \quad \eta_T = 85\%$$

$$W_P' = 4 \text{ kJ/kg}, \quad \eta_P = 70\%$$

$$\eta_{th} = 30\%$$

required: Q_A

$$\eta_{th} = \frac{W_T' - W_P'}{Q_A}$$

$$\eta_T = \frac{W_T'}{W_T}$$

$$0.85 = \frac{650 \text{ kJ/kg}}{W_T}$$

$$W_T = 764.7059 \text{ kJ/kg}$$

$$\eta_P = \frac{W_P}{W_P'}$$

$$0.70 = \frac{W_P}{4 \text{ kJ/kg}}$$

$$W_P = 2.8 \text{ kJ/kg}$$

subst;

$$0.30 = \frac{(764.7059 - 2.8) \text{ kJ/kg}}{Q_A}$$

$$Q_A = 2539.6063 \text{ kJ/kg}$$

$$\Delta h = m_s (h_2 - h_1)$$

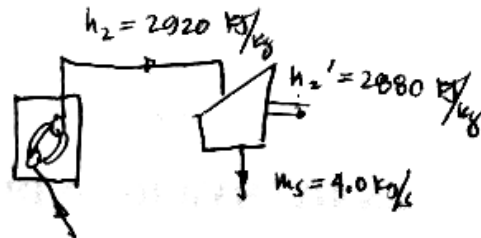
$\swarrow$ $\searrow$
 $h_1 = h_f @ 60^\circ\text{C} = 334.91 \text{ kJ/kg}$
 1300 kJ/kg

$$\Delta h = (1300 - 334.91) \text{ kJ/kg}$$

$$\Delta h = 965.09 \text{ kJ/kg}$$

$$\begin{aligned} W_{NET} &= W_T - W_P \\ &= (3.5 \text{ kg/s}) (3500 - 30) \text{ ft/kg} \end{aligned}$$

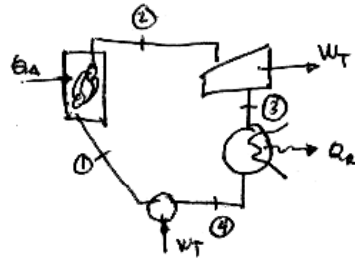
$$W_{NET} = 12145 \text{ ft/s}$$



$$\text{Heat loss} = m_5 (h_2 - h_2') = (4.0 \text{ kg/s})(2920 - 2880) \text{ kJ/kg}$$

$$\text{Heat loss} = 160 \text{ kW}$$

$$\eta_{th} = 1 - \frac{h_3 - h_4}{h_2 - h_1}$$



$$h_2 = h_{g@4\text{MPa}} = 2801.4 \text{ kJ/kg}$$

$$s_2 = s_3 = s_f + x_3 s_{fg}$$

$$6.0701 \text{ kJ/kg-K} = 1.1143 \text{ kJ/kg-K} + x_3 (6.4422 \text{ kJ/kg-K})$$

$$x_3 = 0.7693$$

$$h_3 = h_f + x_3 h_{fg} = 350.54 \text{ kJ/kg} + (0.7693)(2299.3 \text{ kJ/kg})$$

$$h_3 = 2119.3257 \text{ kJ/kg}$$

$$h_4 = 350.54 \text{ kJ/kg}$$

$$h_1 - h_4 = v_4 (p_1 - p_4)$$

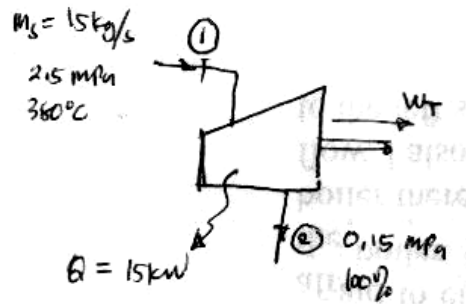
$$h_1 - 350.54 \text{ kJ/kg} = (1.0316 \times 10^{-3} \text{ m}^3/\text{kg})(4000 - 55) \text{ kPa}$$

$$h_1 = 354.6097 \text{ kJ/kg}$$

therefore;

$$\eta_{th} = 1 - \frac{(2119.3257 - 350.54) \text{ kJ/kg}}{(2801.4 - 354.6097) \text{ kJ/kg}}$$

$$\eta_{th} = 27.71\%$$



$$[t_{in} = \text{const}]$$

$$h_1 = h_2 + Q + W_T$$

$$(15 \text{ kg/s})(3194.4 \text{ kJ/kg}) = (15 \text{ kg/s})(2693.6 \text{ kJ/kg}) + 15 \text{ kW} + W_T$$

$$W_T = 7497 \text{ kW}$$

$$\eta_T = \frac{W_T'}{W_T}$$

$$W_T' = (0.80)(1300 \text{ kJ/kg}) = 1040 \text{ kJ/kg}$$

then;

$$4500 \text{ kJ/s} = m_s (1040 \text{ kJ/kg})$$

$$m_s = 4.3269 \text{ kg/s}$$

in terms of kg/kW-hr

$$m_s = 4.3269 \frac{\text{kg}}{\text{s}} \left(\frac{3600 \text{ s}}{1 \text{ hr}} \right) \left(\frac{1}{4500 \text{ kW}} \right)$$

$$m_s = 3.4615 \text{ kg/kW-hr}$$

$$Q_c = Q_w$$

$$m_s (h_2 - h_1) = m_w C_p \Delta T$$

$$(15 \text{ kg/s})(2690 - 290) \text{ kJ/kg} = m_w (4.187 \text{ kJ/kg}\cdot\text{K})(30 - 15)^\circ\text{C}$$

$$m_w = 573.2028 \text{ kg/s}$$

$$\dot{Q}_g = \dot{Q}_w$$

$$m_g C_{pg} \Delta T = m_w C_p \Delta T$$

$$R = \frac{\dot{Q}}{\dot{M}} = \frac{8.3143 \text{ kJ/kg-K}}{30 \text{ kg/s}} = 0.2771 \text{ kJ/kg-K}$$

$$k = \frac{C_p}{C_v} ; R = C_p - C_v$$

$$R = C_p - \frac{C_p}{k}$$

$$R = C_p \left(1 - \frac{1}{k}\right)$$

$$0.2771 \text{ kJ/kg-K} = C_p \left(1 - \frac{1}{1.33}\right)$$

$$C_p = 1.1169 \text{ kJ/kg-K}$$

subst;

$$(0.90 \text{ kg/s})(1.1169 \text{ kJ/kg-K})(160 - 75)^\circ\text{C} = (0.60 \text{ kg/s})(4.1187 \text{ kJ/kg-K})(T_2 - 288 \text{ K})$$

$$T_2 = 322.0111 \text{ K}$$

$$t_2 = 49.0111^\circ\text{C}$$

$$h_T = \frac{w_T'}{w_T}$$

$$w_T = h_1 - h_2$$

$$S_1 = S_2 = S_f + \chi_2 S_{fg}$$

$$7.0573 \text{ kJ/kg} = 1.1453 \text{ kJ/kg} + \chi_2 (6.3867 \text{ kJ/kg})$$

$$\chi_2 = 0.9257$$

$$h_2 = h_f + \chi_2 h_{fg}$$

$$= 359.86 \text{ kJ/kg} + (0.9257)(2299.3 \text{ kJ/kg})$$

$$h_2 = 2488.2615 \text{ kJ/kg}$$

subst;

$$w_T = (3564.2 - 2488.2615) \text{ kJ/kg}$$

$$w_T = 1075.9385 \text{ kJ/kg}$$

Hence;

$$0.85 = \frac{w_T'}{1075.9385 \text{ kJ/kg}}$$

$$w_T' = 914.5477 \text{ kJ/kg}$$

$$\eta_f = \frac{W_T'}{W_T} = \frac{h_1 - h_2'}{h_1 - h_2}$$

$$S_2 = S_1 = S_f + \chi_2 S_{fg}$$

$$6.9646 \text{ kJ/kg} = 0.8931 \text{ kJ/kg} + \chi_2 (6.9383 \text{ kJ/kg})$$

$$\chi_2 = 0.8751$$

$$\begin{aligned} h_2 &= h_f + \chi_2 h_{fg} \\ &= 271.93 \text{ kJ/kg} + (0.8751)(2346.13 \text{ kJ/kg}) \end{aligned}$$

$$h_2 = 2325.1074 \text{ kJ/kg}$$

Hence;

$$0.90 = \frac{3593.8 \text{ kJ/kg} - h_2'}{(3593.8 - 2325.1074) \text{ kJ/kg}}$$

$$h_2' = 2451.9767 \text{ kJ/kg}$$

$$h_f = \frac{w_T'}{w_T} = \frac{h_1 - h_2'}{h_1 - h_2}$$

$$S_2 = S_1 = S_f + X_2 S_{fg}$$

$$1.4361 \text{ Btu/lb-R} = 0.3359 \text{ Btu/lb-R} + X_2 (1.3969 \text{ Btu/lb-R})$$

$$X_2 = 0.7876$$

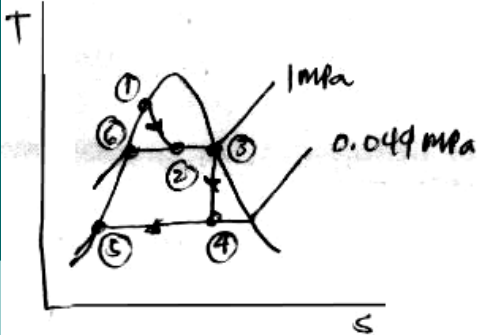
$$h_2 = h_f + X_2 h_{fg} = 196.2 \text{ Btu/lb} + (0.7876)(960.2 \text{ Btu/lb})$$

$$h_2 = 952.4535 \text{ Btu/lb}$$

subst;

$$0.02 = \frac{(1202.4558 \text{ Btu/lb} - h_2')}{(1202.4558 - 952.4535) \text{ Btu/lb}}$$

$$h_2' = 997.4539 \text{ Btu/lb}$$



$$\dot{W}_T = \dot{m}_s (h_3 - h_4)$$

$$h_3 = h_g @ 1.0 \text{ MPa} = 2778.1 \text{ kJ/kg}$$

$$s_3 = s_4 = s_f + x_4 s_{fg}$$

$$s_f @ 0.049 \text{ MPa} = 1.0536 \text{ kJ/kg-K}$$

$$s_{fg} @ 0.049 \text{ MPa} = 6.5839 \text{ kJ/kg-K}$$

$$s_3 = s @ 1.0 \text{ MPa} = 6.5865 \text{ kJ/kg-K}$$

$$x_4 = 0.8404$$

$$h_4 = h_f + x_4 h_{fg}$$

$$h_f @ 0.049 \text{ MPa} = 327.26 \text{ kJ/kg}$$

$$h_{fg} @ 0.049 \text{ MPa} = 2313.4 \text{ kJ/kg}$$

$$h_4 = 2271.4414 \text{ kJ/kg}$$

Solving for $\dot{m}_s$,

$$50000 \text{ MW} = \dot{m}_s (2778.1 - 2271.4414) \text{ kJ/kg}$$

$$\dot{m}_s = 98.6858 \text{ kg/s}$$

for the mass flow rate of the well water

$$\dot{m}_g = \frac{\dot{m}_s}{x} ; \quad h_1 = h_2 = h_f + x_2 h_{fg}$$

$$h_1 = h_f @ 200^\circ\text{C} = 858.45 \text{ kJ/kg}$$

$$h_f @ 1.0 \text{ MPa} = 762.81 \text{ kJ/kg}$$

$$h_{fg} @ 1.0 \text{ MPa} = 2015.3 \text{ kJ/kg}$$

$$x_2 = 0.04747$$

hence;

$$\dot{m}_g = \frac{98.6858 \text{ kg/s}}{0.04747}$$

$$\dot{m}_g = 2079.4803 \text{ kg/s}$$

$$m_s = X m_g = (0.14)(48 \text{ kg/s})$$

$$m_s = 6.72 \text{ kg/s}$$