

Answer Key

ENGINEERING MATHEMATICS

Refresher 02



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$$(x^{12} + 3) \text{ DIVIDED BY } (x - \sqrt{6})$$

Remainder theorem

$$(x^{12} + 3) \text{ subst } x = \sqrt{6}$$

$$[(\sqrt{6})^{12} + 3]$$

$$\text{Remainder} = 46,659$$

$$n = 12$$

$$r = 5$$

$$n - r = 7$$

$$p = 0.70$$

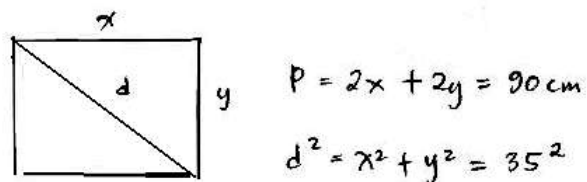
$$q = 0.30$$

Hence;

$$P = {}^n C_r p^r q^{n-r}$$

$$= {}^{12} C_5 (0.70)^5 (0.30)^7$$

$$P = 0.02911$$



Area of Rectangle

$$A = xy$$

$$2x + 2y = 90$$

$$x + y = 45 \longrightarrow (1)$$

$$x^2 + y^2 = 35^2$$

$$x^2 + y^2 = 1225 \longrightarrow (2)$$

Squaring both sides of eq. (1)

$$(x + y)^2 = 45^2$$

$$x^2 + 2xy + y^2 = 2025$$

Substituting eq. (2)

$$1225 + 2xy = 2025$$

$$2xy = 800$$

Hence;

$$A = xy = \frac{800}{2}$$

$$A = 400 \text{ cm}^2$$

4



Congruent angle

5



Lumen

6



Impulse

7

Associative law

8



Solid

9



Rhombus

ARITHMETIC MEAN

$$A_m = \frac{a_1 + a_2 + \dots + a_n}{n}$$

$$A_m = \frac{3a + 4b}{2}$$

$$\frac{3x^2 - 32x - 50}{(x-1)(x-2)(x+3)} = \frac{A}{x-1} + \frac{B}{x-2} + \frac{C}{x+3}$$

multiply both sides of equation by $(x-1)$

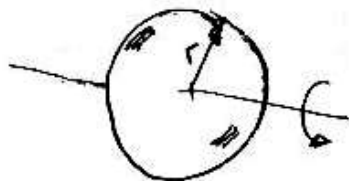
$$\frac{3x^2 - 32x - 50}{(x-2)(x+3)} = A + (x-1) \left[\frac{B}{x-2} + \frac{C}{x+3} \right]$$

subst; $x=1$

$$A = \frac{3(1)^2 - 32(1) - 50}{(1-2)(1+3)}$$

$$A = \frac{79}{4}$$

moment of inertia



$$\begin{aligned}
 I_{sp} &= \frac{2}{5} m r^2 \\
 &= \frac{2}{5} \frac{(0.8 \text{ lb}_s)}{(32.2 \text{ ft/s}^2)} (1.50 \text{ in})^2 \left(\frac{1 \text{ ft}}{12 \text{ in}}\right)^2
 \end{aligned}$$

$$I_{sp} = 1.5528 \times 10^{-4} \text{ ft} \cdot \text{lb} \cdot \text{sec}^2$$

$$R_x = \frac{1}{5}$$

$$R_y = \frac{1}{7}$$

$$R_z = \frac{1}{9}$$

How long will it take to do the job if
X and Y work for 2 days then Y and Z
finish the job

$$(R_x + R_y)2 + (R_y + R_z)T = 1$$

$$\left(\frac{1}{5} + \frac{1}{7}\right)2 + \left(\frac{1}{7} + \frac{1}{9}\right)T = 1$$

$$T = 1.2375$$

if X and Y finish the job for 2 days and
Y and Z added 1.2375 days then

X, Y and Z can finish the job in 3.2375 days

Find integral of $12 \sin^7 x \cos^7 x dx$ from limit of 0 to $\pi/2$
from Wall's formula

$$\int_0^{\pi/2} \sin^m u \cos^n u du = \frac{[(m-1)(m-3)\dots \frac{2}{1}][(n-1)(n-3)\dots \frac{2}{1}] \alpha}{(m+n)(m+n-2)(m+n-4)\dots \frac{2}{1}}$$

$$\alpha = \frac{\pi}{2} \text{ IF both } m \text{ and } n \text{ are even}$$

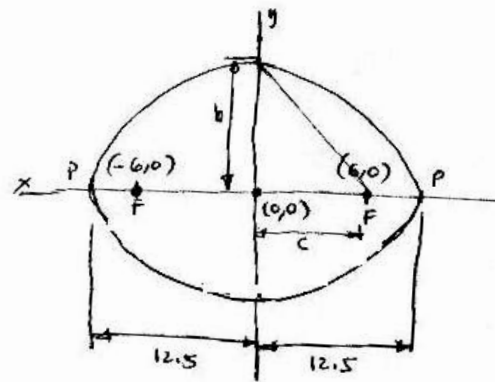
$$\alpha = 1 \text{ IF otherwise}$$

$m=7$ and $n=7$ are both odd, then $\alpha = 1$

$$m+n = 14$$

$$= 12 \left[\frac{\{6 \times 4 \times 2\} \{6 \times 4 \times 2\} (1)}{(14)(12)(10)(8)(6 \times 4 \times 2)} \right]$$

$$= 0.0429$$



$$\text{eccentricity} = e = \frac{c}{a} < 1$$

$$a^2 = b^2 + c^2$$

$$12.5^2 = b^2 + 6^2$$

$$b^2 = 120.25$$

$$b = 10.9659$$

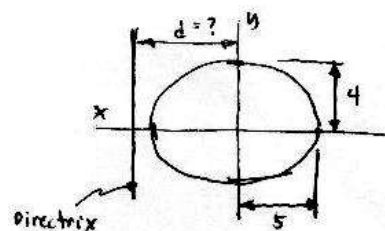
$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

Hence;

$$a > b$$

$$\left(\frac{x}{12.5}\right)^2 + \left(\frac{y}{10.9659}\right)^2 = 1$$

distance from the center to the directrix



$$e = \frac{a}{d} = \frac{c}{a}$$

$$d = \frac{a^2}{c} ; a^2 = b^2 + c^2$$

$$5^2 = 4^2 + c^2$$

$$c = 3$$

subst; $d = \frac{5^2}{3}$

$$d = 8 - \frac{1}{3}$$

$$d = 8.3333$$

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Boyle's law

18

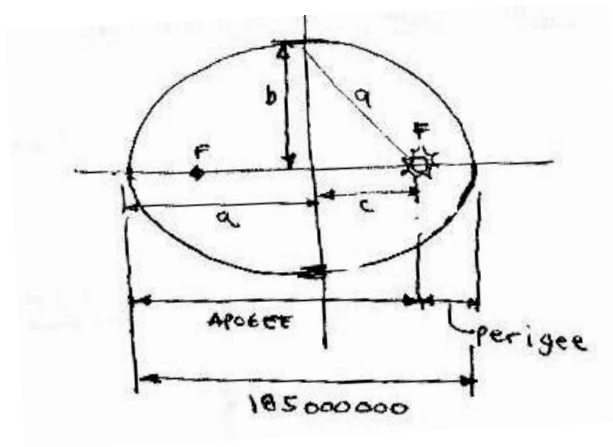


Centrifugal force

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Congruent



$$e = \frac{c}{a} = \frac{1}{70}$$

Find The Apogee of the earth

$$\text{Apogee} = a + c$$

$$a = \frac{185000000}{2} = 92500000$$

from eccentricity

$$\frac{c}{a} = \frac{1}{70}$$

$$c = (92500000) \left(\frac{1}{70} \right)$$

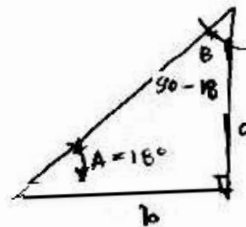
$$c = 1321428.571$$

Hence;

$$\text{Apogee} = 185000000 + 1321428.571$$

$$\text{Apogee} = 186,321,428.6 \text{ miles}$$

$$\tan(9F + 1) = \cot(18)$$



Relationships:

$$\cot A = \frac{b}{a} \Rightarrow \tan B = \frac{b}{a}$$

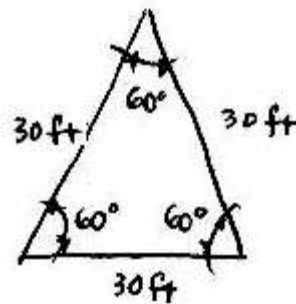
$$\cot 18^\circ = \frac{b}{a} \Rightarrow \tan 72^\circ = \frac{b}{a}$$

Subst;

$$\cancel{\tan}(9F + 1) = \cancel{\tan} 72^\circ$$

$$9F + 1 = 72^\circ$$

$$F = 7.8889^\circ$$



Problem: Largest triangular area that can be fenced in

$$A = \frac{1}{2} b a \sin \theta$$
$$= \frac{1}{2} (30 \text{ ft})(30 \text{ ft}) \sin 60^\circ$$

$$A = 389.7114 \text{ ft}^2$$

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$$\text{Probability} = \frac{\text{No. of favorable ways}}{\text{No. of possible ways}}$$

Number of favorable ways of getting a sum of 9

D ₁	D ₂	D ₃
1	2	6
	3	5
	4	4
	5	3
	6	2

5 ways

D ₁	D ₂	D ₃
2	1	6
	2	5
	3	4
	4	3
	5	2
	6	1

6 ways

D ₁	D ₂	D ₃
3	1	5
	2	4
	3	3
	4	2
	5	1

5 ways

D ₁	D ₂	D ₃
4	4	1
	3	2
	2	3
	1	4

4 ways

D ₁	D ₂	D ₃
5	1	3
	2	2

2 ways

25 Favorable ways that the sum of 3 dice is 9

Number of favorable ways of getting a sum of 11

D ₁	D ₂	D ₃
1	6	4
	5	5
	4	6

3 ways

D ₁	D ₂	D ₃
2	6	3
	5	4
	4	5
	3	6

4 ways

D ₁	D ₂	D ₃
3	6	2
	5	3
	4	4
	3	5
	2	6

5 ways

D ₁	D ₂	D ₃
4	6	1
	5	2
	4	3
	3	4
	2	5
	1	6

6 ways

D ₁	D ₂	D ₃
5	5	1
	4	2
	3	3
	2	4
	1	5

5 ways

D ₁	D ₂	D ₃
6	4	1
	3	2
	2	3
	1	4

4 ways

27 favorable ways that the sum of 3 dice is 11

$$\text{Number of favorable ways} = 27 + 25 = 52$$

Since 3 dice will fall (1 die has 6 faces)
 $(6)(6)(6) = 216$ # of possible ways

thus:

$$P = \frac{52}{216}$$

$$P = 0.2407$$

$$\text{Probability} = \frac{\text{No. of favorable ways}}{\text{No. of possible ways}}$$

Probability of Randomly drawing 11 white and 7 black

$$P_{(1W \text{ and } 1B)} = \frac{(11C_1)(7C_1)}{18C_2}$$

$$P_{(1W \text{ and } 1B)} = 0.5033$$

$$r = 600 \text{ ft}$$

$$f = 0.18$$

$$v = 70 \text{ mph}$$

Solution: $\tan(\theta + \phi) = \frac{v^2}{gr}$

$$v = \left(70 \frac{\text{mi}}{\text{hr}}\right) \left(\frac{1 \text{ hr}}{3600 \text{ s}}\right) \left(\frac{5280 \text{ ft}}{1 \text{ mi}}\right) = 102.6667 \text{ ft/sec}$$

$$\tan(\theta + \phi) = \frac{(102.6667 \text{ ft/sec})^2}{(32.2 \text{ ft/sec}^2)(600 \text{ ft})}$$

$$\theta + \phi = 28.6156^\circ$$

$$\text{from: } \tan \phi = f = 0.18$$

$$\phi = 10.2039^\circ$$

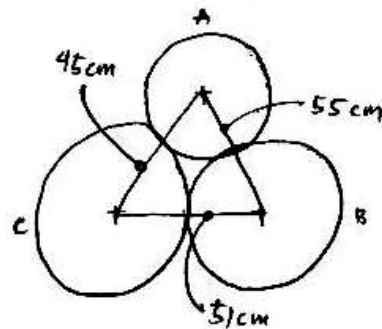
$$\theta + 10.2039^\circ = 28.6156^\circ$$

$$\theta = 18.4116^\circ$$

Hence, the coefficient of friction that sliding will impend

$$\tan \theta = \tan(18.4116^\circ)$$

$$f = 0.3330$$



$$r_A + r_B = 55$$

$$r_C + r_B = 51$$

$$r_C + r_A = 45$$

Using Calculator:

$$r_A = 24.5 \text{ cm}$$

$$r_B = 30.5 \text{ cm}$$

$$r_C = 20.5 \text{ cm}$$

Hence; Diameters

$$d_A = 49 \text{ cm}$$

$$d_B = 61 \text{ cm}$$

$$d_C = 41 \text{ cm}$$

$$x + y = 8 \longrightarrow (1)$$

$$x^3 + y^2 = M \longrightarrow (2)$$

Subst eq(1) to (2)

$$y = 8 - x$$

$$x^3 + (8 - x)^2 = M$$

$$x^3 + 64 - 16x + x^2 = M$$

$$\frac{dM}{dx} = 3x^2 - 16 + 2x = 0$$

Solve for x ;

$$x = 2 \quad ; \quad x = -8/3 \text{ (disregard)}$$

$$y = 6$$

Hence; $x = 2$ and $y = 6$

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Cable

29



Point

30



Critical point

31



Variables

32



Notes receivables

33



Cash

34

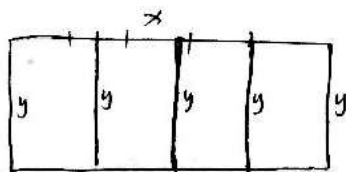


All of these

35



Freight-in



Fencing length of 1800 ft

Find the largest field that can be fenced this way

Area is to be maximized

$$2x + 5y = 1800$$

$$A = xy$$

Subst;

$$x = \frac{1800 - 5y}{2}$$

$$A = \left(\frac{1800 - 5y}{2} \right) y$$

$$\frac{dA}{dy} = 900y - \frac{5}{2}y^2$$

$$\frac{dA}{dy} = 900 - \frac{10}{2}y = 0$$

$$y = 180$$

$$x = 450$$

Hence;

$$A = xy = (450)(180) \text{ ft}^2$$

$$A = 81000 \text{ ft}^2$$

$$\text{Probability} = \frac{\text{Number of favorable ways}}{\text{Number of possible ways}}$$

Number is even:

$$P = \frac{50}{100} = \frac{1}{2}$$

Number is above 70:

$$P = \frac{30}{100} = 0.30$$

Number is even or above 70

$$P = \frac{1}{2} + 0.30 - \left(\frac{1}{2}\right)(0.30)$$

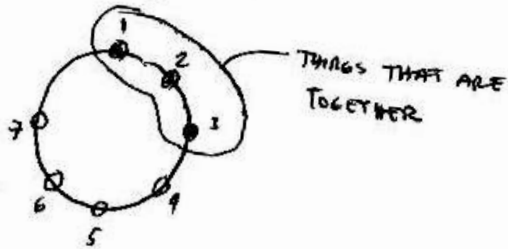
→ Bec. above 70, there are still even numbers

$$P = \frac{13}{20}$$

$$P = 0.65$$

Circular Permutation

$$N = (n-1)!$$

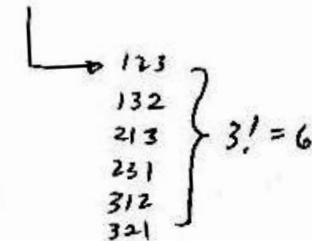


TOTAL permutation

$$N = (7-1)! = 720$$

w/ 3 people not in consecutive order

$$N = (5-1)! \cdot 3! = 144$$

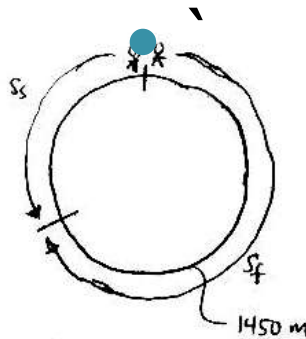


Hence;

$$N = 720 - 144$$

$$N = 576 \text{ ways}$$

39



let v_f = be the faster

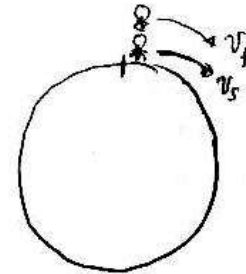
v_s = be the slower

"they meet every 4 minutes"

$$s_f + s_s = 1450 \text{ m}$$

$$(4)v_f + (4)v_s = 1450 \text{ m}$$

$$v_f + v_s = 362.5 \text{ m/min} \rightarrow \text{eq 1}$$



"they come abreast every 32 minutes"

$$32v_f - 32v_s = 1450 \text{ m}$$

$$v_f - v_s = 45.3125 \text{ m/min} \rightarrow \text{eq 2}$$

by elimination and substitution to solve for v_f ;

$$v_f = \left(203.9063 \frac{\text{m}}{\text{min}}\right) \left(\frac{1 \text{ km}}{1000 \text{ m}}\right) \left(\frac{60 \text{ min}}{1 \text{ hr}}\right)$$

$$v_f = 12.2344 \text{ kph}$$

	GOLD	SILVER	BAR OF GOLD AND SILVER
IN AIR	20	12	$x + y = 105$
	x	y	
IN WATER	19	11	$\frac{19}{20}x + \frac{11}{12}y = 99$
	$\frac{19}{20}x$	$\frac{11}{12}y$	

every 20 kilos of
GOLD in AIR loses
1 kilo in WATER

every 12 kilos of silver
in AIR loses 1 kilo
in WATER

Solving for x and y

$$\left. \begin{array}{l} x = 82.5 \text{ kg} \\ y = 22.5 \text{ kg} \end{array} \right\} \text{ in air}$$

$$\left. \begin{array}{l} x = 78.375 \text{ kg} \\ y = 20.625 \text{ kg} \end{array} \right\} \text{ in water}$$

Hence;

$$x = 82.5 \text{ kg}$$

$$\begin{array}{ccc} (x + 3y - z)^3 \\ \downarrow \quad \downarrow \quad \downarrow \\ [1 + 3(1) - 1]^3 \end{array}$$

$$\text{Sum of coefficients} = 27$$

$$V = (298.3 \text{ cm}^3) \left(\frac{1 \text{ m}}{100 \text{ cm}} \right)^3 = 2.983 \times 10^{-4} \text{ m}^3$$

$$T = 100^\circ\text{C} + 273 = 373 \text{ K}$$

$$m = (0.852 \text{ gr}) \left(\frac{1 \text{ kg}}{1000 \text{ gr}} \right) = 8.52 \times 10^{-4} \text{ kg}$$

$$P = 120 \text{ kPa}$$

from: $PV = nRT$

$$(120 \text{ kPa})(2.983 \times 10^{-4} \text{ m}^3) = n(8.314 \text{ kJ/kg mol} \cdot \text{K})(373 \text{ K})$$

$$n = 1.1543 \times 10^{-5} \text{ kg mol}$$

Hence;

$$MW = \frac{m}{n} = \frac{8.52 \times 10^{-4} \text{ kg}}{1.1543 \times 10^{-5} \text{ kg mol}}$$

$$MW = 73.8115 \text{ kg/kg mol}$$

43



Sales discount

44



Optics

45



Ampere

46



Dyne

47



Permutation

48



It quadruples

49



Are similar

50



Complementary angles

51



Base

52



Treasury bills or t-bills

53



Golden handshake

54



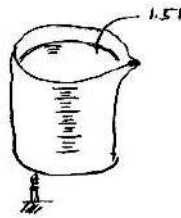
Bars of gold

Linear expansion: $\Delta L = \alpha L_0 \Delta T$

Area Expansion: $\Delta A = 2\alpha A_0 \Delta T$

Volume Expansion: $\Delta V = 3\alpha V_0 \Delta T$

α = coefficient of linear expansion



$$t_1 = 23^\circ\text{C}$$

$$t_2 = 90^\circ\text{C}$$

$$\alpha_{\text{pyrex}} = 3 \times 10^{-6} / ^\circ\text{C}$$

$$\alpha_{\text{water}} = 72 \times 10^{-6} / ^\circ\text{C}$$

Required: Amount of water overflows

$$\text{Amount of water overflows} = \Delta V_{\text{water}} - \Delta V_{\text{pyrex}}$$

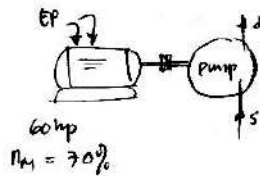
$$= 3 V_0 \Delta T (\alpha_{\text{water}} - \alpha_{\text{pyrex}})$$

$$= 3 (1.5\text{L}) (90 - 23)^\circ\text{C} (72 \times 10^{-6} - 3 \times 10^{-6}) / ^\circ\text{C}$$

$$= (0.0202\text{L}) \left(\frac{1\text{m}^3}{1000\text{L}} \times \frac{100\text{cm}}{1\text{m}} \right)^3$$

$$\text{Amount of water overflows} = 20.20\text{ cm}^3$$

56



$$\begin{aligned} N &= 950 \text{ rpm} \\ \eta_p &= 85\% \\ Q &= 6.0 \text{ ft}^3/\text{sec} \\ SG &= 0.738 \end{aligned}$$

Find: specific speed

$$N_s = 51.63 \frac{\text{rpm} \sqrt{Q, \text{m}^3/\text{s}}}{(\text{TDH}, \text{m})^{3/4}}$$

$$\eta_m = \frac{BP}{EP} \times 100\%$$

$$\begin{aligned} 0.70 &= \frac{BP}{60 \text{ hp}} \\ BP &= 42 \text{ hp} \end{aligned}$$

subst;

$$0.85 = \frac{WP}{42 \text{ hp}}$$

$$WP = (35.7 \text{ hp}) \left(\frac{0.746 \text{ kW}}{1 \text{ hp}} \right) = 26.6322 \text{ kW}$$

from;

$$WP = Q \gamma_{\text{liq}} \text{TDH}$$

$$26.6322 \text{ kW} = \left(6.0 \frac{\text{ft}^3}{\text{sec}} \right) \left(\frac{1 \text{ m}}{3.28 \text{ ft}} \right)^3 \left(9.81 \frac{\text{kN}}{\text{m}^3} \right) (0.738) \text{TDH}$$

$$\text{TDH} = 21.6348 \text{ m}$$

Hence;

$$N_s = 51.63 \frac{(950 \text{ rpm}) \sqrt{0.17 \text{ m}^3/\text{s}}}{(21.6348 \text{ m})^{3/4}}$$

$$N_s = 2015.9768 \text{ rpm}$$

work problem

$$\frac{n_1 T_1}{W_1} = \frac{n_2 T_2}{W_2}$$

TO EXCAVATE:

$$\frac{(8)(8)}{16} = \frac{(10)(x)}{25}$$

$$x = 10 \text{ hrs}$$

TO BACKFILL:

$$\frac{(3)(5)}{12} = \frac{(10)y}{25}$$

$$y = 3.125 \text{ hrs}$$

total time to excavate & backfill

$$x + y = 13.125 \text{ hrs}$$

$$C_0 = \text{P}130,000$$

$$L = 8 \text{ yrs}$$

$$\text{Resale value} = \text{P}25,000$$

$$Q/M = \text{P}2,400 ; \text{increased by } \text{P}600 \text{ each year}$$

$$i = 17\%$$

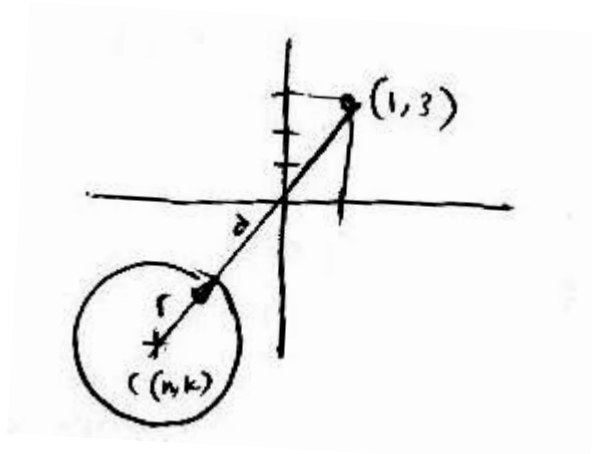
Ownership in terms of Present Worth

$$PW = C_0 + \left(A + \frac{G}{i} \right) \left[\frac{1 - (1+i)^{-N}}{i} \right] - \frac{NG}{i} (1+i)^{-N}$$

$$= \text{P}130,000 + \left(\text{P}2,400 + \frac{\text{P}600}{0.17} \right) \left[\frac{1 - (1+0.17)^{-8}}{0.17} \right] - \frac{(8)(\text{P}600)}{0.17} (1+0.17)^{-8}$$

$$PW = \text{P}146,905.0848$$

59



$$D = d + r$$

$$d = D - r$$

Solving for r ;

$$(x^2 + 12x + 36) + (y^2 + 8y + 16) = -30 + 36 + 16$$

$$(x+6)^2 + (y+4)^2 = 22$$

$$C(-6, -4) ; r = 4.6904$$

Distance Formula

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(1+6)^2 + (3+4)^2}$$

$$D = 9.8995$$

Hence;

$$d = 9.8995 - 4.6904$$

$$d = 5.2091 \text{ units}$$

Probability of Drawing A Black King and an Ace in Succession

$$P_{\text{black}} = \frac{2}{52}$$

$$P_{\text{ace}} = \frac{4}{52}$$

note: keywords "And" use
multiplication

"or" use addition

Hence;

$$P = \left(\frac{2}{52}\right)\left(\frac{4}{52}\right)$$

$$P = 0.002959$$

61

$$D_1 = 4 \text{ cm}$$

$$N_1 = 250 \text{ rpm}$$

$$P_1 = 65 \text{ kW}$$

$$D_2 = 3 \text{ cm}$$

$$N_2 = 350 \text{ rpm}$$

$$P_2 = ?$$

$$P \propto N \propto D^3$$

$$P = kND^3$$

$$65 \text{ kW} = k(250 \text{ rpm})(4 \text{ cm})^3$$

$$k = \frac{13}{3200} \frac{\text{kW}}{\text{rpm} \cdot \text{cm}^3}$$

Hence;

$$P = \left(\frac{13}{3200} \frac{\text{kW}}{\text{rpm} \cdot \text{cm}^3} \right) (350 \text{ rpm})(3 \text{ cm})^3$$

$$P = 38.3906 \text{ kW}$$

$$₹45000 = (₹15000 - ₹1000) \left[\frac{1 - (1+i)^{-10}}{i} \right] + ₹2500(1+i)^{-10}$$

Trial and error or using calculator:

$$i = 28.75\%$$

63



Barter

64



Auction

65



Embargo

66



Idle money

67



Variance

68



Directrix

69

$2.99792 \times 10^3 \text{ m/s}$

70



Subtrahend

$$C_0 = \text{P} 300,000$$

$$C_L = \text{P} 35,000$$

$$L = 10 \text{ yrs}$$

Straight Line Depreciation Method

$$C_5 = C_0 - nd$$

$$d = \frac{C_0 - C_L}{L} = \frac{\text{P} 300,000 - \text{P} 35,000}{10} = \text{P} 26,500$$

Hence,

$$C_5 = \text{P} 300,000 - (5)(\text{P} 26,500)$$

$$C_5 = \text{P} 167,500$$

$$e_i = \left(1 + \frac{i_n}{m}\right)^m - 1$$

$$= \left(1 + \frac{0.08}{2}\right)^2 - 1$$

$$e_i = 8.16\% \text{ effective annual rate}$$

Hence;

$$A \left[\frac{(1.04)^{40} - 1}{0.04} \right] = \text{P} 12000 \left[\frac{(1.0816)^6 - 1}{0.0816} \right]$$

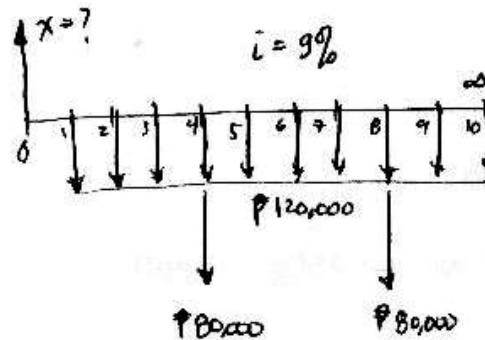
$$A = \text{P} 930.1406$$

$$P = F(1 + i)^{-N}$$
$$= \text{P}15,000 \left(1 + \frac{0.05}{4}\right)^{-4(10)}$$

$$P = \text{P}9,126.20$$

$$P = ₱1800 \left[\frac{1 - (1.06)^{-50}}{0.06} \right]$$

$$P = ₱28\,371.3492$$

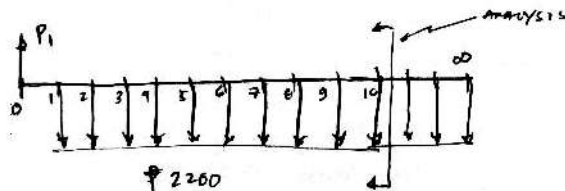


$$\text{CAPITALIZED COST} = \frac{P120,000}{0.09} + \frac{P80,000}{(1.09)^4 - 1}$$

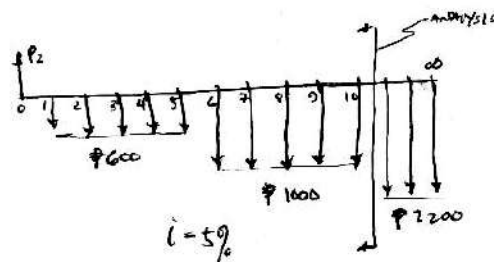
$$\text{CAPITALIZED COST} = P1,527,705.477$$

76

OLD MAINTENANCE COST



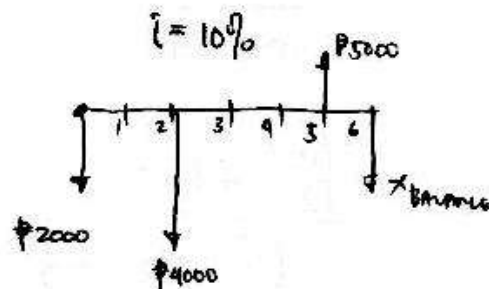
DUE TO PLACEMENT OF NEW PAVEMENT
NEW MAINTENANCE COST



Comparison is 10 years period only

$$P_2 = ₱600 \left[\frac{1 - (1.05)^{-5}}{0.05} \right] + ₱1000 \left[\frac{1 - (1.05)^{-5}}{0.05} \right] (1.05)^{-5}$$

$$P_2 = ₱5989.9443$$



$$X = P4000(1.10)^5 + P2000(1.10)^6 - P5000(1.10)^1$$

$$X = P4485.162$$

$$F = P(1+i)^N$$
$$= \text{₱}480(1.15)^8$$

$$F = \text{₱}1468.3310$$

79



Entrepreneur

80



Consol

81



Imaginary numbers

82



D

Discounted Payback Period

$$P = A \left[\frac{1 - (1+i)^{-N}}{i} \right] \quad i = 19\%$$

$$₱28,000 = ₱16,000 \left[\frac{1 - (1.19)^{-N}}{0.19} \right]$$

using calculator:

$$N = 2.3237 \text{ years}$$

CAPITALIZED COST OF EQUIPMENT = ₱150,000

$$i = 13\%$$

$$C_L = ₱8000$$

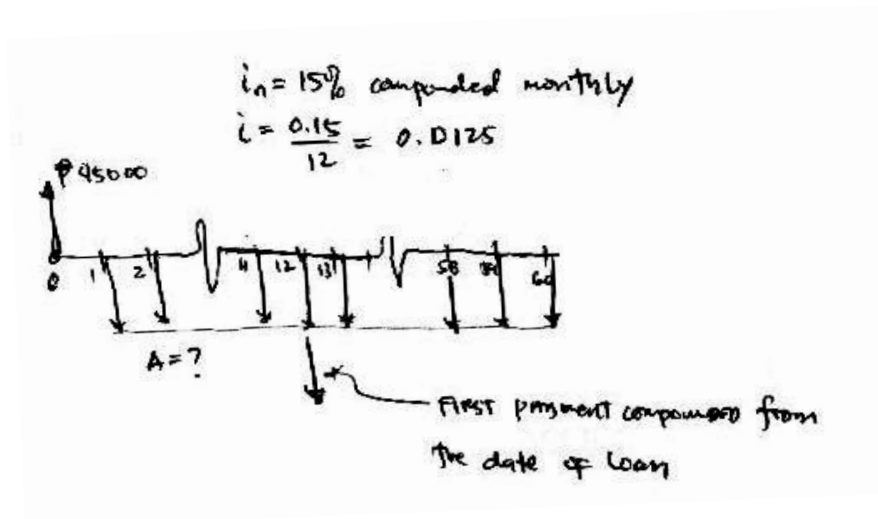
$$L = 10 \text{ yrs}$$

Replacement Cost of Equipment

$$CC = C_0 + P_{o/m} + \frac{C_0 - C_L}{(1+i)^N - 1}$$

$$₱150,000 = C_0 + 0 + \frac{C_0 - ₱8000}{(1.13)^{10} - 1}$$

$$C_0 = ₱108,168.4546$$



$$A \left[\frac{1 - (1.0125)^{-60}}{0.0125} \right] (1.0125)^{-11} = P45,000$$

$$A = P1227.300$$

86



Mode

87



Pentagon

88



Segment

89

Scientific notation

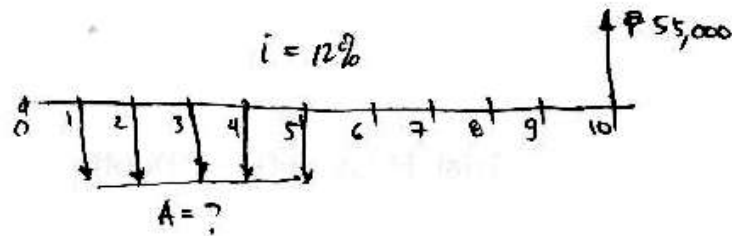
90



Spherical segment

91

Bisector of an angle



$$A \left[\frac{(1.12)^5 - 1}{0.12} \right] = P 55,000 (1.12)^{-5}$$

$$A = P 4,912,5180$$

$$\begin{aligned} I &= Pin \\ &= (\text{P}12,000)(0.15)(1) \\ I &= \text{P}1800 \end{aligned}$$

Then,

$$\text{P}12,000 - \text{P}1800 = \text{P}10200$$

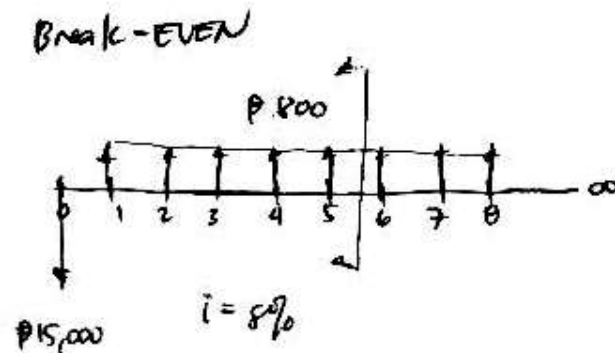
and from

$$F = P(1 + in)$$

$$\text{P}12,000 = \text{P}10200 [1 + (i)(1)]$$

$$i = 0.1765$$

$$i = 17.65\%$$

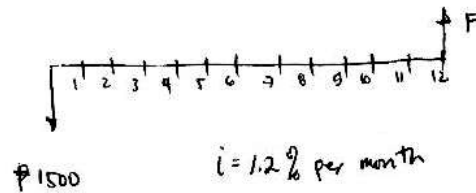


$$[Income = Expenses]$$

$$X + P800 \left[\frac{(1.08)^5 - 1}{0.08} \right] = P15,000 (1.08)^5$$

$$X = P17,346.6404$$

95

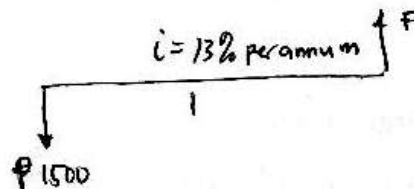


$$I_1 = F - P$$

$$F = P1500(1.012)^{12} = P1730.8419$$

$$I_1 = P1730.8419 - P1500$$

$$I_1 = P230.8419$$



$$I_2 = F - P$$

$$F = P1500(1.13)^1 = P1695$$

$$I_2 = P1695 - P1500$$

$$I_2 = P195$$

Hence;

$$\text{Savings} = I_1 - I_2$$

$$= P230.8419 - P195$$

$$\text{Savings} = P35.8419$$

96

Exterior angle

97



Curve

98



Inscribed

Operating in Corrosive Atmosphere

$$C_0 = \text{P}450$$

$$L = 6 \text{ years}$$

If treated for Corrosion Resistance

$$C_0 = \text{P}800$$

$$L = ? \quad i = 8\%$$

$$\left[\begin{array}{c} \text{Capitalized cost for} \\ \text{untreated} \end{array} = \begin{array}{c} \text{Capitalized cost for} \\ \text{treated} \end{array} \right]$$

$$\text{P}450 + \frac{\text{P}450}{(1.08)^6 - 1} = \text{P}800 + \frac{\text{P}800}{(1.08)^N - 1}$$

$$N = 13.9215 \text{ years}$$

100

Break-even Point

$$PW_{\text{Plan A}} = PW_{\text{Plan B}}$$

$$₱100,000 = ₱75,000 + ₱50,000 (1.09)^{-N}$$

$$N = 8.0432 \text{ years}$$